



gamlss2: The Next Generation of Distributional Regression

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<http://nikum.org>

The GAMLSS Journey

- Similar to GLMs, GAMLSS are strongly related to the IWSM.
- **2001**, first GAMLSS talk by Mikis and Bob at the IWSM 2001 in Odense, DK:
"The GAMLSS project: A Flexible Approach to Statistical Modelling".
- **20** years ago, 2005-06-24, first CRAN *gamlss* package.
- **2005**, JRSS C., doi:10.1111/j.1467-9876.2005.00510.x



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Generalized Additive Models for Location, Scale and Shape

R. A. Rigby ✉, D. M. Stasinopoulos

Journal of the Royal Statistical Society Series C: Applied Statistics, Volume 54, Issue 3, June

2005, Pages 507–554, <https://doi.org/10.1111/j.1467-9876.2005.00510.x>

Published: 14 April 2005

- **2007**, JSS, doi:10.18637/jss.v023.i07

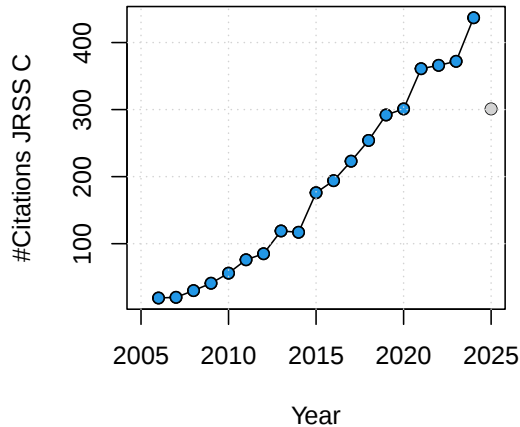
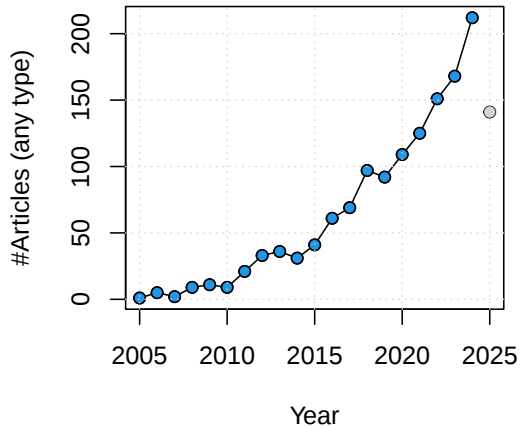


Generalized Additive Models for Location Scale and Shape (GAMLSS) in R

D. Mikis Stasinopoulos, Robert A. Rigby

The GAMLSS Journey

Google Scholar queries (GAMLSS + distributional regression):

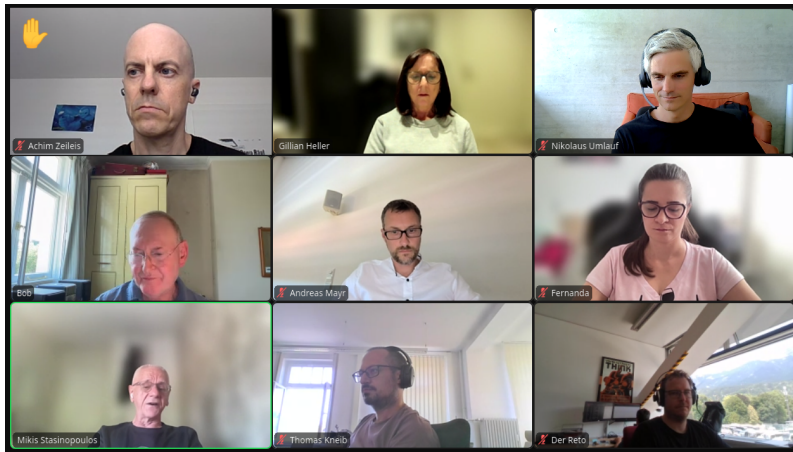


The GAMLSS Journey

- R package *gamlss*: flexible regression for location, scale, shape.
- Limitations in existing R packages (*gamlss*, *VGAM*, *mgcv*, *bamlss*)
- Need for extensibility, custom families, custom algorithms, efficiency, etc.
- **July 2023**,
IWSM Dortmund, first discussions on how to improve the *gamlss* software.
- **September 2023**,
started first function for processing arbitrary complex formulae.
- **December 2025**,
first "proof of concept" of *gamlss2*.

The GAMLSS Journey

The **GAMLSS** Working Party:



Installation

The *gamlss2* package is provided at

<https://github.com/gamlss-dev/gamlss2>

Install with:

```
install.packages("gamlss2",  
  repos = c("https://gamlss-dev.R-universe.dev",  
            "https://cloud.R-project.org"))
```

CRAN version coming soon!



Main Function

```
gamlss2(formula, data, family = NO,  
         subset, na.action, weights, offset, start = NULL,  
         control = gamlss2_control(...), ...)
```

- **Modular design** facilitating easy development of new features.
- Use of **Formula** package for **arbitrary complex formulae**.
- Use of **mgcv** `smooth.construct()`.
- Easy development of **new families**, `?gamlss2.family`.
- **New special model term** design, `?special_terms`.
- Model fitting function is **exchangeable**, `?gamlss2_control`, `?RS`.
- Support for **large data** sets, argument `binning = TRUE`.
- **Improved** `predict()` method.
- Use of **topmodels** package for post-estimation results.

Spirometry Data

- Paper published in 2025.
- "Simple models match GAMLSS in accuracy but are easier to use".
- Spirometry measurements from NHANES 2007-2012, $n = 16596$.

Original Research

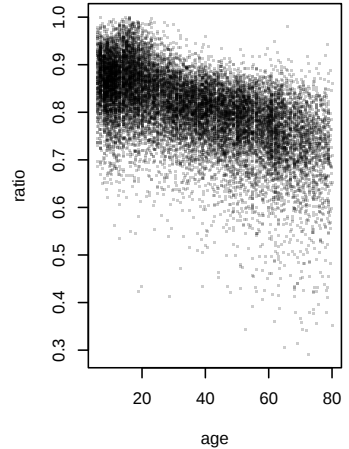
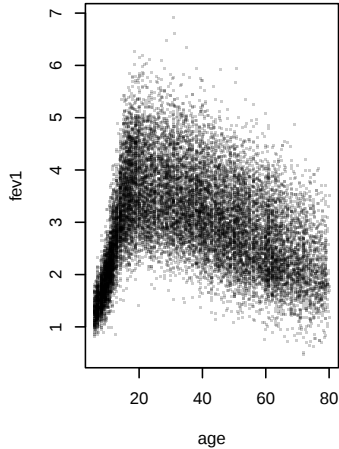
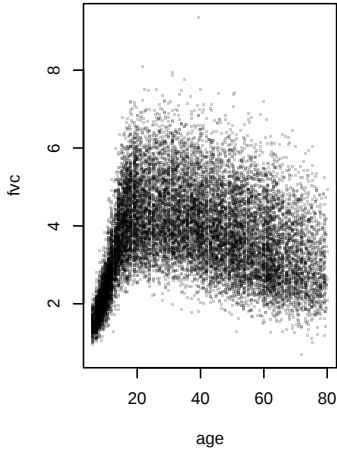
Debunking the
GAMLSS myth:
Simplicity reigns in
pulmonary function
diagnostics

```
R> data("SpirometryUS", package = "gamlss2")  
R> head(SpirometryUS, 3)
```

	fvc	fev1	ratio	pef	fef	volume	fet	gender	age	weight	height
41475	2.473	2.025	0.8188435	5.755	2.119	94	8.7	female	62.50	138.9	154.7
41476	1.742	1.551	0.8903559	3.635	2.122	50	5.4	female	6.75	22.0	120.4
41479	3.545	2.957	0.8341326	8.932	4.081	100	10.5	male	52.50	65.7	154.4
	bmi	ethnicity									
41475	58.04	other									
41476	15.18	other									
41479	27.56	mexican									

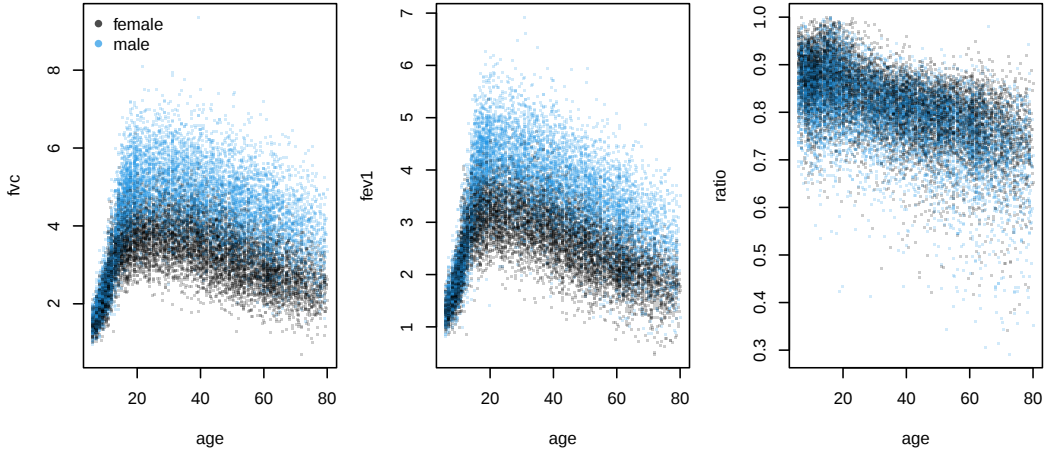
Spirometry Data

Spirometry Measurements from NHANES 2007-2012.



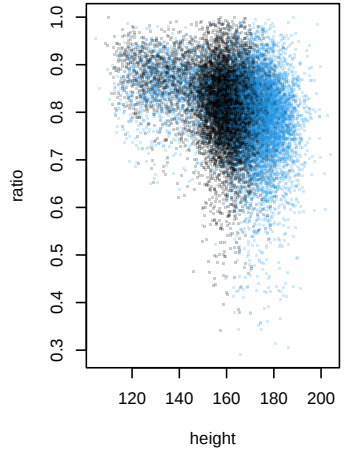
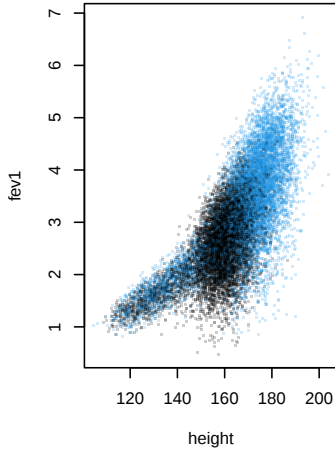
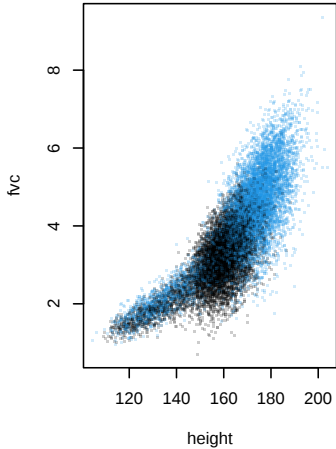
Spirometry Data

Spirometry Measurements from NHANES 2007-2012.



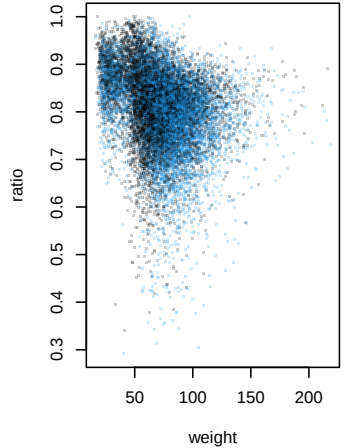
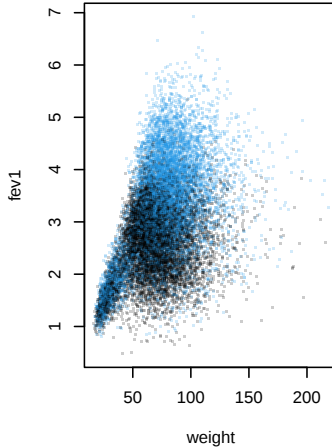
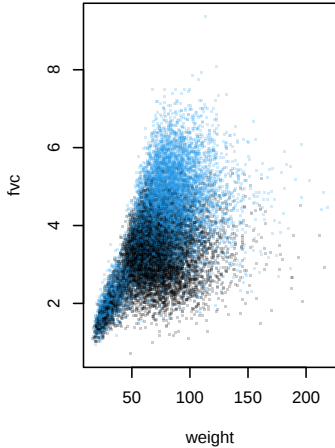
Spirometry Data

Spirometry Measurements from NHANES 2007-2012.



Spirometry Data

```
d <- subset(SpirometryUS, gender == "female")
```



Families

Simplified "gamlss2.family" class, inspired by *bamlss* and *distributions3*.

```
R> ND <- function(...) {  
+   rval <- list(  
+     "family" = "Normal Distribution",  
+     "names" = c("mu", "sigma"),  
+     "links" = c(mu = "identity", sigma = "log"),  
+     "pdf" = function(y, par, log = FALSE) {  
+       dnorm(y, mean = par$mu, sd = par$sigma, log = log) },  
+     "cdf" = function(y, par, ...) {  
+       pnorm(y, mean = par$mu, sd = par$sigma, ...) },  
+     "quantile" = function(p, par) {  
+       qnorm(p, mean = par$mu, sd = par$sigma) }  
+   )  
+   class(rval) <- "gamlss2.family"  
+   rval  
+ }
```

Additionally: `random()`, `mean()`, `variance()`, `z_weights(y, eta, peta, j), ...`

Estimation

Model formula.

```
R> f <- fev1 ~ s(age) | s(age)
R> f <- fev1 ~ s(age) + s(height) + s(weight) | s(age)
R> f <- fev1 ~ s(age) + s(height) + s(weight) | . | 1
R> f <- fev1 ~ s(age) + s(height) + s(weight) + te(height, weight) | .
```

Estimation using the new family.

```
m1 <- gamlss2(f, family = ND, data = d)
GAMLSS-RS iteration 15: Global Deviance = 7101.8205 eps = 0.000008
```

Faster with *gamlss.dist* family NO().

```
m2 <- gamlss2(f, family = NO, data = d)
GAMLSS-RS iteration 12: Global Deviance = 7083.5112 eps = 0.000008
```

Finding a Model

Several options for finding a model:

- Set `ridge = TRUE` in `gamlss2()`, for ridge penalty for linear effects.
- Special model term `la()` for Lasso penalized terms.
- Stepwise model term selection `step_gamlss2()`, `stepwise()`.
- Double shrinkage penalty `select_gamlss2()`, `sRS()`.
- Find distribution and model terms with `find_gamlss2()`.

Search using selected distributions implemented in *gamlss.dist*.

```
R> f <- fev1 ~ s(age) + s(height) + s(weight) + te(age, weight) | . | . | .  
R> m <- find_gamlss2(f, data = d, select = TRUE, k = log(nrow(d)),  
+   families = c("NO", "JSU", "BCPE"), mu.link = "log")
```

Finding a Model

```
summary(m)
```

```
Call:
```

```
gamlss2(formula = formula, data = ..1, family = families[[j]],  
  ... = pairlist(trace = FALSE, mu.link = "log", criterion = "BIC",  
  criterion_refit = "BIC", select = TRUE, thres = c(0.9, 0.2), optimizer = sRS))
```

```
---
```

```
Family: BCPE
```

```
Link function: mu = log, sigma = log, nu = identity, tau = log
```

```
*-----
```

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)	
mu.(Intercept)	0.914677	0.001854	493.32	<2e-16	***
sigma.(Intercept)	-1.928581	0.005623	-343.00	<2e-16	***
nu.(Intercept)	1.470509	0.033103	44.42	<2e-16	***
tau.(Intercept)	0.649488	0.013509	48.08	<2e-16	***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Finding a Model

Smooth terms:

	mu.s(age)	mu.s(height)	mu.s(weight)	mu.te(age,weight)	sigma.s(age)
edf	7.7968	1.1599	5.7635	19.2724	1.8732

	sigma.te(age,weight)
edf	4.826

*-----

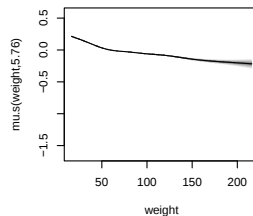
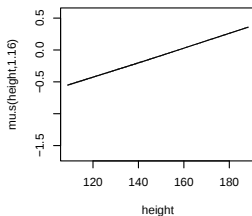
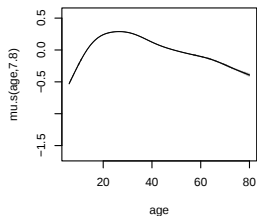
n = 8303 df = 44.69 res.df = 8258.31

Deviance = 6861.7347 Null Dev. Red. = 60.39%

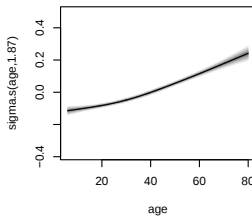
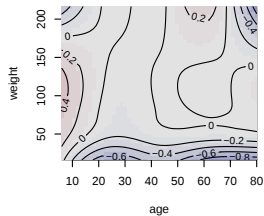
AIC = 6951.1185 elapsed = 34.94sec

Estimated Effects

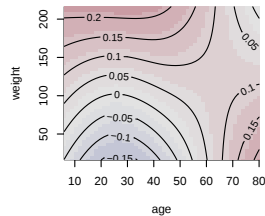
```
R> plot(m)
```



$\mu.s(\text{age}, \text{weight}, 19.27)$



$\sigma.s(\text{age}, \text{weight}, 4.83)$



Diagnostics

Support of the *topmodels* package for probabilistic model assessment.

```
R> library("topmodels")
```

Q-Q plots for quantile residuals.

```
R> qqrpplot(m)
```

Probability integral transform (PIT) histograms.

```
R> pithist(m)
```

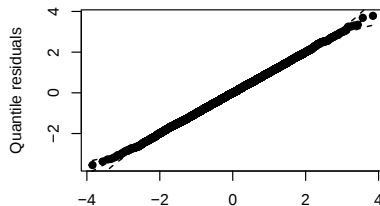
Rootogram, compare (square roots) of empirical frequencies with expected (fitted) frequencies.

```
R> rootogram(m)
```

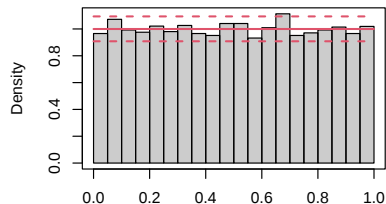
Worm plots using quantile residuals.

```
R> wormplot(m)
```

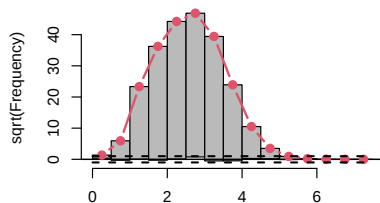
Diagnostics



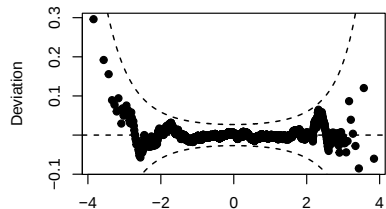
Theoretical quantiles



PIT



fev1



Theoretical quantiles

Special Model Terms

Several special model terms implemented:

- Smooth terms from *mgcv*: `s()`, `te()`, `ti()`.
- Smooth terms from *gamlss*: `pb()`, etc.
- Lasso penalized terms: `la()`, `plot_lasso()`.
- Neural networks from *nnet*: `n()`.
- Trees and forests from *partykit*: `tree()`, `cf()`.
- Loess smoothing: `lo()`.

New specials can be implemented with (see `special_terms`):

- Generic fitting method: `special_fit(x, ...)`.
- Generic predict method: `special_predict(x, ...)`.

Special Model Terms

Example: Segmented regression (linear B-spline with free knots).

```
R> fk <- function(x, ...) {  
+   sx <- list()  
+   ## ...  
+   class(sx) <- c("special", "fk")  
+   return(sx)  
+ }  
R> special_fit.fk <- function(x, ...) {  
+   sx <- list()  
+   ## ...  
+   class(sx) <- "fk.fitted"  
+   return(sx)  
+ }  
R> special_predict.fk.fitted <- function(x, ...) {  
+   ## ...  
+   return(p)  
+ }
```

Special Model Terms

In action:

```
f <- fev1 ~ I(age^2) + I(height^2) + weight + I(age * height^2) + fk(age, k = 3)
b <- gamlss2(f, data = d, family = NO)
```

GAMLSS-RS iteration 3: Global Deviance = 8016.1594 eps = 0.000001

Compare:

```
R> AIC(m1, m2, m, b)
```

	AIC	df
m	6951.119	44.69194
m2	7175.344	45.91658
m1	7207.094	52.63670
b	8034.159	9.00000

Predictions

```
R> nd <- data.frame(
+   "age" = seq(6, 80, by = 1),
+   "height" = 140,
+   "weight" = 40
+ )

R> par <- predict(m, newdata = nd)
R> head(par, 4)

      mu      sigma      nu      tau
1 1.666610 0.1272847 1.470509 1.91456
2 1.734938 0.1266004 1.470509 1.91456
3 1.805685 0.1259245 1.470509 1.91456
4 1.877806 0.1252619 1.470509 1.91456

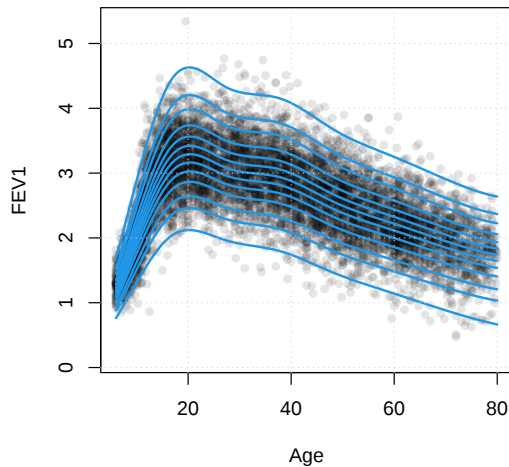
R> q5 <- family(m)$quantile(0.05, par)
R> head(q5)

[1] 1.297166 1.352547 1.409959 1.468576 1.527030 1.583589

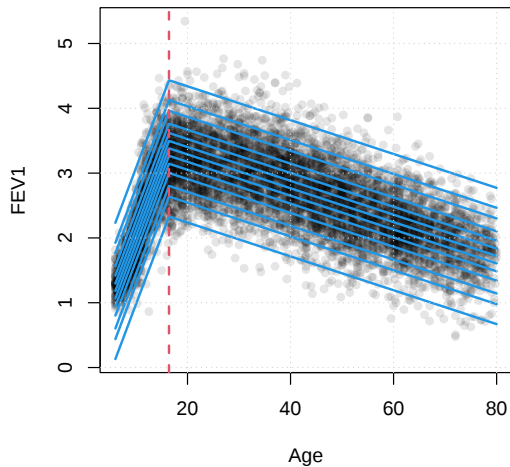
R> qu <- quantile(m, newdata = nd, probs = seq(0.01, 0.99, by = 0.01))
```

Predictions

GAMLSS

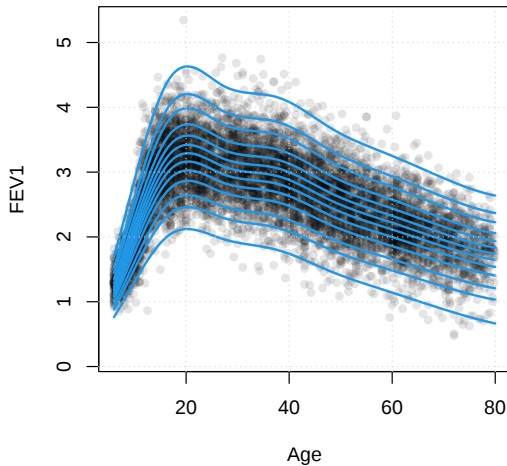


Segmented

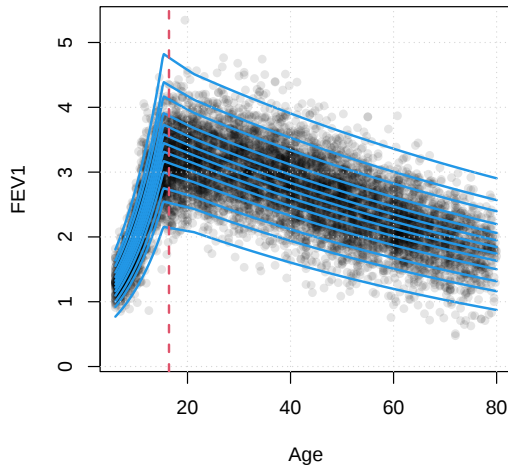


Predictions

GAMLSS



GAMLSS Segmented



Lasso

Lasso model terms are implemented via `la()`:

```
la(x, type = 1, const = 1e-05, ...)
```

- `type = 1`: simple lasso penalty.
- `type = 2`: group lasso penalty.
- `type = 3`: ordinal fusion penalty.
- `type = 4`: nominal fusion penalty.

Example: Factor fusion, create factor variable first.

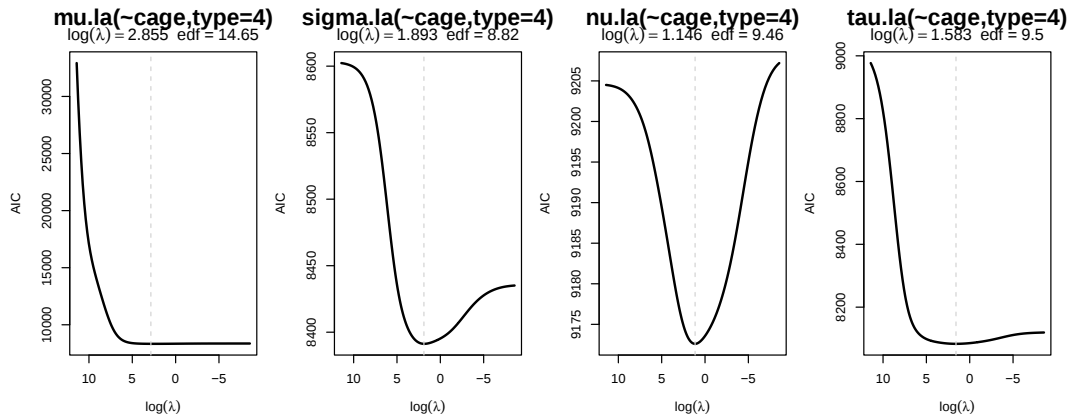
```
R> d$cage <- cut(d$age, breaks = seq(6, 80, by = 2), include.lowest = TRUE)
```

Estimate GAMLSS Lasso model.

```
R> m4 <- gamlss2(fev1 ~ la(~cage, type = 4) | . | . | ., data = d,  
+ family = BCPE(mu.link = "log"), criterion = "AIC", add_ridge = TRUE)
```

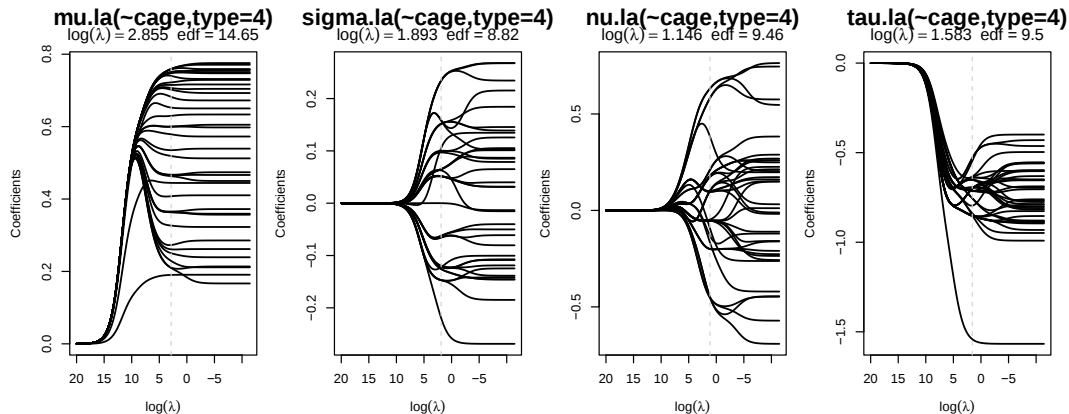
Lasso

Visualize using `plot_lasso(..., which = "criterion")`.



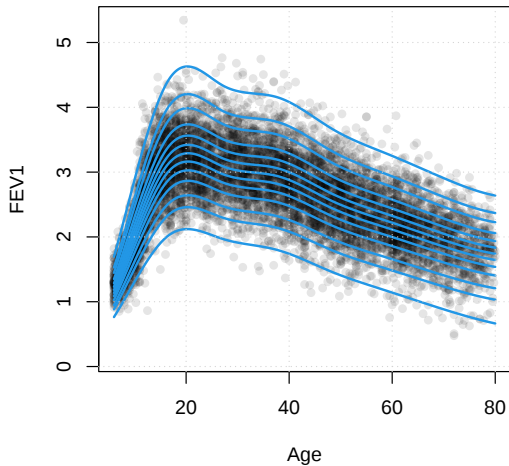
Lasso

Visualize using `plot_lasso(..., which = "coefficients")`.

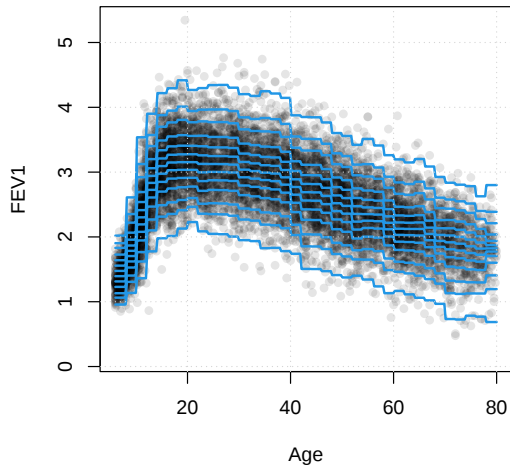


Lasso

GAMLSS



GAMLSS Lasso



Summary

- *gamlss2*: modular framework for flexible distributional regression.
- Supports smooth terms, lasso, custom families, large datasets, a.o.
- Example: Spirometry data - model selection, estimation, diagnostics, prediction.
- Exchangeable estimation engines and integration with *topmodels* for post-estimation tools.

Thank you! Questions welcome.